

CECS 528, LO Assessment 1, Fall 2026, Dr. Ebert

IMPORTANT: For each problem (LO1,LO2,GK,Advanced, All LO Makeups) write your solution using a **SINGLE** and **SEPARATE SHEET OF PAPER (FRONT AND BACK)**. Write your **FIRST NAME, ALPHABETIZING NAME** and **PROBLEM NUMBER** on each sheet.

25 Points Each

- LO1**
- a. Use the Master Theorem to determine the growth of $T(n)$ if it satisfies the recurrence $T(n) = 9T(n/3) + 1000n^2 + n$. Defend your answer. (10 pts)
 - b. Use the Substitution method to establish that, if $T(n) = T(n/5) + T(n/4) + n$, then $T(n) = \Theta(n)$. Note: this proves that the **Find Statistic** algorithm requires $O(n)$ steps. (15 pts)

- LO2**
- a. Demonstrate the **Median-of-Five Find Statistic Algorithm** when applied to the array

$$a = 86, 96, 35, 16, 36, 94, 55, 50, 77, 8, 44, 15, 19, 32, 55, 98, 68, 78, 70, 7, 3, 20, 87$$

with $k = 7$, lower = 0, and upper = 22. Compute the pivot M , the arrays a_{left} and a_{right} , and the updated lower and upper values. Hint: although you do not need to show the step by step details, nevertheless you should be applying the partitioning algorithm from Hoare's **Quicksort**.

- b. What is its worst-case running time of Hoare's **Quicksort** and what must happen in order for it to occur? Explain and defend your answer using an arithmetic series and evaluating the growth of that series. (13 pts)

- GK**
- a. Using just a few sentences, why is the Master Theorem by itself insufficient for determining the big-O number of steps that is needed to execute any arbitrary divide-and-conquer algorithm? (10 pts)
 - b. For a uniform divide-and-conquer recurrence, what do the a , b , and $f(n)$ represent assuming that $T(n)$ is describing the number of steps that are needed to execute some divide-and-conquer algorithm?

- ADV**
- a. Consider an array $a = (x_1, y_1), \dots, (x_n, y_n)$ of two-dimensional points where each component is an integer. Describe in a paragraph an $O(n)$ algorithm that takes a as input along with a value k , $0 \leq k < n$, and returns the k points of a that are furthest from the origin $(0, 0)$, where distance is calculated using the Euclidean distance:

$$\sqrt{x_1^2 + x_2^2}.$$

Hint: you may use any of the algorithms that were covered presented in the Divide and Conquer lecture. (10 points)

- b. Convert your paragraph description to rigorous pseudocode. Make sure to clearly define all variables and all functions that are being called. (15 pts)